

## RESEARCH ON THE BREEDING VALUE ESTIMATION FOR BEEF TRAITS BY A SIMPLIFIED MIXED MODEL

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### Abstract

*The paper purpose was to apply a simplified mixed model BLUP for estimating bulls' breeding value for meat production in terms of weight daily gain and establish their hierarchy. Also, it aimed to compare the bulls' ranging obtained by a simplified BLUP mixed model with their hierarchy set up by contemporary comparison. A sample of 1,705 half sibs steers, offspring of 106 Friesian bulls were used as biological material. Bulls' breeding value varied between + 244.5 g for the best bull and -204.7 g for the bull with the weakest records. A number of 57 bulls ( 53.77%) registered positive breeding values. The accuracy of the breeding value estimation varied between 80, the highest precision, in case of the bull number 21 and 53, the lowest precision, in case of the bull number 38. A number of 7 bulls of the total of 57 with a positive breeding value were situated approximately on the same positions at a difference of 0 to 1 points on the both lists established by BLUP and contemporary comparison. As a conclusion, BLUP could be largely and easily applied in bull evaluation for meat production traits in term of weight daily gain, considered the key parameter during the fattening period and its precision is very high, a guarantee that the bulls' hierarchy is a correct one. If a farmer would chose a high breeding value bull from a catalogue, he could be sure of the improvement of beef production by genetic gain.*

*Key words:* breeding value estimation, bulls ranging, meet production traits, simplified mixed model

### INTRODUCTION

Selection of the best animals, needed to induce genetic gain, requires to estimate their breeding value, which allows to establish their ranging according to their genetic superiority. The accuracy of the breeding value estimation is the key aspect to which many researchers paid attention. The precision depends on the number of measurements, number of offspring and heritability of the traits. The higher the number of measurements, the number of descendants and heritability, the higher the accuracy of the breeding value [22].

The best modern method considered to assure a correct estimation of the breeding value with the highest precision is BLUP Animal Model and its present variants. The mixed model BLUP was established by [20,21] and later it was improved by other researchers. It is a linear unbiased mathematical model destined to minimize the error of breeding value estimate.

Its advantages consists of: (a) the reduction of time and cost of the data processing, (b) the reduction of the error of breeding value estimate, (c) the increased accuracy of the breeding value estimate, (d) the facilitation of the assessment of breeding value of sires and dams based on the records used for family selection, (e) the facilitation of an increased selection precision due to the use of multi trait genetic and environment correlations between various characters [9,31,32,41,56].

BLUP is widely used to estimate breeding value in various animals species and breeds: in dairy cattle [1,4,6,14,26,33,34,37,45,46,50], in beef cattle [3,7,12,13,16,35,37,39,42,43], in swine [5,25,38], in poultry [27,54], in horses [2,48,57], in sheep and goats [3,10,18,53], in fishes [29,47], in honey bee [8], in dogs [23]. Also, this subject was theoretically approached by many other authors [28,40,44,51]. Due to its advantages, BLUP was also used in the prediction of breeding value and estimation of single nucleotide

polymorphism (SNPs) [1,17, 30], in cross under dominance [24], in small populations with long-term objectives where selection procedures put less emphasis on family information [52], in the field of ecology to estimate the genetic component of phenotypic variation as a tool for ecologists [55].

The use of BLUP was also successfully extended to plant breeding and variety testing [36].

During the last half of century, animal and plant production carried out remarkable records by means of the genetic improvement [15,16,49].

The evolution mathematical models used in breeding value estimation was marked by the substantial contribution given by two researchers: Charles Henderson, who established BLUP mixed models and Robin Thompson, who sustained the Residual Maximum Likelihood (The REML), a method for variance component estimation [15,19,49]. The BLUP implementation was facing difficulties due to the limitations of the computers performance in the period 1972-1995. Later, it has been easily applied due to the performance registered in the field of computing techniques and equipment.

In the field of cattle breeding, BLUP was successfully used for the evaluation of many breeds such as Angus, Hereford, Polled Herford, Shorthorn, Limousin, Red Angus in the USA based on various sire models (1971-1984). After 1984, the BLUP model included the additive maternal effect [7,16]. Later, the RAM models (reduced animal models) were largely used based on birth weight and weaning weight as well as weaning weight and post weaning weight [49].

In this context, the paper approached the topic of breeding value estimation for beef production traits of Friesian bulls using a simplified mathematical model of BLUP in Romania, where contemporary comparison was applied for a long period.

**MATERIALS AND METHODS**

In order to set up this research work, a sample of 1,705 half sibs steers, offspring of 106

Friesian bulls were used as biological material. The bulls were randomly selected and it was considered that there is no relationship between them.

The sire breeding value estimation was based on the records of their offspring during the fattening period, in term of weight daily gain, considered one of the main selection characters.

The breeding value was assessed using a simplified BLUP mixed model, a linear mathematical model having the form:

$$Y_{ij} = \mu + s_i + e_{ij}, \quad (1)$$

where  $Y_{ij}$  = the record of the  $j$  offspring of the bull  $i$ ,  $\mu$  is a fixed unknown parameter,  $s_i = 1/2 g_i$ , where:  $g_i$  – the „ $i$ ” bull’s breeding value ( $j=1, \dots, n_{ij}$ ),  $e_{ij}$  = the residual effect,  $s$  and  $e$  are non correlated variables among them with the averages equal to zero and variances  $\sum_s^2$  and  $\sum_e^2$ .

Considering  $\sum(e_{ij}) = 0, cov(e_{ij}, e_i, j,) = 0$ , if  $i \neq i'$ , or at least  $j \neq j'$  and  $\sum_{ij}^2 = \sum_e^2$ . The linear model does not suppose that bulls are relatives among them,  $cov(s_i, s_i) = 0, \sum_{si}^2 = \sum_s^2 = 1/4 \sum_A^2$ .

Considering that  $n_i$  represents the number of decendants of the “ $i$ ” bull, then the equations of the mixed model are:

$$\begin{bmatrix} n & n_1 & n_2 & \dots \\ n_1 n_1 + \sum_e^2 / \sum_s^2 & 0 & \dots & \dots \\ n_2 & 0 & n_2 + \sum_e^2 / \sum_s^2 & \dots \\ \dots & \dots & \dots & \dots \end{bmatrix} \begin{bmatrix} \mu \\ s_1 \\ s_2 \\ \dots \end{bmatrix} = \begin{bmatrix} y_{..} \\ y_1 \\ y_2 \\ \dots \end{bmatrix} \quad (2)$$

The breeding value of the “ $i$ ” bull,  $s_i$ , will be:

$$s_i = 2(n_i/n_i + a) (y_i - \mu) \quad (3)$$

where:  $s = \sum_e^2 / \sum_s^2$ . If we consider  $n_i/(n_i+a) = w_i$ , then  $\bar{\mu} = \sum w_i \bar{y}_i / \sum w_i$ .

The precision of the estimated breeding value,  $R^2$ , was calculated using the formula:

$$R^2 = w_i - \frac{w_i}{\sum w_i} \quad (4)$$

When  $n_i$  has a high value, then

$$R^2 = w_i(1 - \frac{1}{\sum w_i}), \text{ unde } \sum w_i \text{ goes to}$$

infinity and  $1/\sum w_i$  goes to zero.

This simplified mixed model was utilized for estimating the bulls breeding value and its precision for daily gain.

The estimated breeding value allowed to establish the bulls hierarchy. The results were compared to the bulls' classification based on the contemporary comparison.

The rank correlation between the two classifications of the bulls was calculated according to the formula:

$$r_s = 1 - \frac{6\sum d^2}{n(n^2 - 1)} \quad (5)$$

The correlation significance was tested for the probabilities  $P = 0.05$  and  $P = 0.01$ , using Fisher Test.

## RESULTS AND DISCUSSIONS

**Bulls' breeding value** varied between + 244.5 g for the best bull and -204.7 g for the bull with the weakest records.

Of the total of 106 bulls evaluated in this experiment, 57 bulls (53.77%) registered positive breeding values, being situated over the average of the sample. The best bull for improving meat production in terms of weight daily gain recorded + 244,5 g and the bull situated on the last position as improver + 2.2.g (Table 1).

**The accuracy of the breeding value estimation** varied between 80, the highest precision, in case of the bull number 21 and 53, the lowest precision, in case of the bull number 38. It deserves to mention that the breeding value of the bull with the number 21 was estimated based on its 30 offspring, while the breeding value estimated in case of the bull number 38 was calculated only based of the records coming from 8 descendants.

The precision values could be explained by the fact that they depended on the offspring

group size per bull, which varied between the optimum limitations, minimum 8-10 descendants per bull.

Table 1. Bulls' breeding value and its precision for meat production trait-weight daily gain- Simplified mixed model BLUP

Bull number	Number of offspring	Breeding Value +BV	Accuracy R <sup>2</sup>
1	22	244.5	75
2	28	181.2	79
3x	17	174.5	70
4x	18	168.2	71
5x	13	162.6	64
6x	18	156.3	71
7x	12	150.1	62
8	23	149.3	76
9	14	113.4	66
10	22	112.2	75
11	12	109.5	62
12	11	108.1	60
13	15	98.6	67
14x	20	98.2	73
15	15	93.5	67
16	22	84.0	75
17	13	82.5	64
18	14	81.6	66
19x	15	75.9	67
20	9	74.0	55
21	30	72.9	80
22	16	72	69
23x	12	64.9	62
24	13	64	64
25	12	63.8	62
26	32	61.4	81
27	16	60.6	69
28	17	58.8	70
29	14	54.0	68
30	25	50.2	77
31	21	50	74
32	24	44.6	76
33	23	43	76
34	10	42.2	58
35	16	41.6	69
36	20	40.6	73
37x	16	39.4	69
38	8	37.6	53
39	24	30.5	76
40	17	23.7	70
41	15	21.5	67
42	13	21.4	64
43x	11	21.1	60
44	15	16.3	67
45	11	15.8	60
46	17	14.2	70
47	12	13.0	52
48	21	12.8	74
49	23	11.4	76
50x	12	10.4	62
51	15	8.8	67
52	14	7.1	66
53	16	6.5	69
54	13	4.9	64
55	13	4.0	64
56	15	2.3	67
57	13	2.2	64

Source: Own calculations

**Bulls' classification based on the simplified mixed model BLUP and contemporary comparison**

Table 2. Comparison between bulls' hierarchy according to their breeding value calculated by the simplified mixed BLUP model and their classification established by contemporary comparison

Bull number	Position occupied according to the method used for breeding value estimation	
	Simplified BLUP mixed model	Contemporary comparison
1	1	19
2	2	20
3xx	3	3
4x	4	5
5	5	2
6	6	10
7x	7	6
8	8	37
9	9	14
10	10	18
11	11	27
12	12	1
13	13	38
14	14	11
15	15	31
16	16	21
17	17	28
18	18	30
19x	19	17
20	20	12
21	21	34
22	22	16
23x	23	22
24	24	15
25	25	53
26	26	44
27	27	35
28	28	32
29	29	4
30	30	46
31	31	9
32	32	47
33	33	50
34	34	24
35	35	43
36	36	51
37x	37	39
38	38	33
39	39	57
40	40	54
41	41	55
42	42	48
43	43	45
44	44	23
45	45	36
46	46	26
47	47	40
48	48	8
49	49	56
50x	50	48
51	51	7
52	52	13
53	53	41
54	54	25
55	55	29
56	56	42
57	57	52

Source: Own calculations

Based on the breeding value estimated by the simplified mixed model BLUP, the bulls were classified in the decreasing order.

Also, their breeding value was calculated by means of the contemporary comparison and again the bulls were classified according to the results obtained by the application of this method.

The comparison between the bulls' classification based on the breeding value calculated by means of the mixed model BLUP and the bulls' hierarchy established based on the contemporary comparison showed that the bulls occupied different positions on the two classification lists because we used two different methods to determine their breeding value.

But, if we look at the first 10 bulls situated on the list established based on the breeding value calculated by the simplified mixed model BLUP, we can select 5 bulls which have almost similar positions on the other list, where their breeding value was calculated by contemporary comparison.

If we take into consideration all the 57 bulls able to improve weigh daly gain, we may notice that 7 bulls are situated aproximately on the same positions on the both classifications at a difference of 0 to 1 positions. It is about the bulls with the number: 3,4,7,19,23,37 and 50. (Table 2).

**The rank correlation** between the positions occupied by bulls on the two classifications based on the breeding value, calculated by means of two methods: simplified mixed model BLUP and contemporary comparison, was  $r = 0.569$ , substantially significant for  $P=0.05$  and  $P=0.01$ , meaning that the use of BLUP modifies in a small measure the positions occupied by bulls in the hierarchy established by means of contemporary comparison.

Crettenand (1975) found closer correlations between these positions, but he considered that BLUP has a higher precision which reflects its superiority compared to contemporary comparison [11].

## CONCLUSIONS

BLUP could be largely and easily applied in bull evaluation for meat production traits in term of weight daily gain, considered the key parameter during the fattening period.

The method assured a high precision ranging between 53 and 80, depending on the number of offspring per bull.

However, it would be better to proceed to the bull selection based on a multiple trait model where many other characters to be taken into consideration such as: body weight at the age of 180 days, body weight at the age of 365 days, and carcass characters as well. Only in this way, breeding value estimation could be more precisely determined. The more characters considered, the higher accuracy in breeding value estimation.

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## REFERENCES

- [1]Ahmad Suasana Aziz, 2010, Application of BLUP in prediction of breeding values and estimation of SNP effects in dairy cattle, Ph.D.Thesis, University of Nottingham, [www.theses.nottingham.ac.uk](http://www.theses.nottingham.ac.uk)
- [2]Arnason, T., Van Vleck L. Dale, 2000, Genetic Improvement of the Horse
- [3]Avendano, S., Villanueva, B., Woolliams, J.A., 2003, Expected increases in genetic merit from using optimized contributions in two livestock populations of beef cattle and sheep, *J. Anim. Sci.*, 81:2964-2975
- [4]Banik, S., Gandhi, R.S., 2006, Animal Model versus Conventional Methods of Sire Evaluation in Sahiwal Cattle, *Asian-Aust. J. Anim. Sci.*, 19(9):1225-1228
- [5]Belonsky, G.M., Kennedy, B.W., 1988, Selection on Individual Phenotype and Best Linear Unbiased Predictor of Breeding value in a closed Swine Herd, *J. Anim. Sci.*, 66:1124-1131
- [6]Ben Gara A., Rekik, B., Boualleque, M., 2006, Genetic parameters and evaluation of the Tunisian dairy cattle population for milk yield by Bayesian and BLUP Analysis, *Livestock Science*, 100(20):142-149
- [7]Benyshek, L.L., 1991, Beef cattle national genetic evaluation programs. *Beef Seedstock Symp.*, South Dakota State University, Brookings

- [8]Bienefeld Kaspar, Ehrhardt Klaus, Reinhardt Friederich, 2007, Genetic evaluation in the honey bee considering queen and worker effects-A BLUP - Animal Model Approach, *Apidologie*, 38(1):77-85
- [9]Bondoc Orville, L., 2008, Animal Breeding, Principles and Practice in the Philippine Context, The University of the Philippines Press.
- [10]Clarke, J.N., 1986, Evaluation of industry breeding programs for sheep and goats. Introduction and Overview. 3rd World Congress on Genetics Applied to Livestock Production
- [11]Crettenand, J., 1975, Le testage de taureaux sur la base d'équations linéaires. Thèse pour l'obtenir du Grade de Docteur en Sciences Techniques, Zurich
- [12]Cunha, E.E., Euclides, R.F., Torres, R.A., Carneiro, P.L.S., 2006, Genetic Evaluation of beef cattle herds through simulated data. *Arquivo Brasileiro de Medicina Veterinaria e Zootecnia*, 58(30):381-387
- [13]Eriksson Jan-Ake, Wilton James W., Henningsson Thore, 1979, Evaluating Performance-Tested Beef Bulls for Daily Gain by BLUP, *Acta Agriculturae Scandinavica*, 29(4):393-401
- [14]Estimated Breeding Value for Beef Cattle-Signet, The Signet Guide to Estimated Breeding Values (EBVS), [www.signetfbc.co.uk/beefbreeders/estimated\\_breeding\\_values\\_for\\_beef\\_cattle.pdf](http://www.signetfbc.co.uk/beefbreeders/estimated_breeding_values_for_beef_cattle.pdf)
- [15]Gilmour, A.R., Mixed models in animal breeding: Where to now/ *Proc. Assoc. Advmt. Anim. Breed. Genet.* 18:394-397
- [16]Golden, B.L., Garrick, D.J., Benyshek, L.L., 2009, Milestones in beef cattle genetic evaluation, *J. Anim. Sci.*, 879140, suppl E3-E10
- [17] Habier, D., Fernando, R.L., Garrick, D.J., 2013, Genomic BLUP decoded: a look into the black box of genomic prediction in Genetics: Early online, published May 2, 2013, [www.genetics.org](http://www.genetics.org)
- [18]Hadfield, J.D., Wilson, A.J., Garant, D., Sheldon, B.C., Krunk, L.E., 2010, The misuse of BLUP in ecology and evolution. *Am. Nat.*, 175(1):116-125
- [19]Henderson, C.R., 1973, Sire evaluation and genetic trends. *Proc. Annu. Breeding Genet. Symp.*, Honor of Dr. J.L. Lush, ASAS and ADSA, Champaign, IL
- [20]Henderson, C.R., 1975, Best linear unbiased estimation and prediction under a selection model. *Biometrics*, 31(2):423-447
- [21]Henderson, C. R., 1984, Applications of Linear Models in Animal Breeding. University of Guelph, Ontario
- [22]Jespersen Charlotte, 2002, Chapter 7. Estimation of indices for breeding value. 04.06.2002, [www.ihh.kvl.dk/genetics](http://www.ihh.kvl.dk/genetics)
- [23]Leighton Eldin A., Booker Jane H., 2003, How to use Estimated Breeding Values to Genetically Improve Dog Guides, Meeting of the "Original Group" Sept.11-12, 2003, Morristown, New Jersey
- [24]Lo, L.L., Fernando R.L., Grossman, M., 1997, Genetic evaluation by BLUP in two-bred terminal crossbreeding systems under dominance. *J. of Animal Sci.*, 75:2877-2884
- [25]Mabry, J.W., See, M.T., 1990, Selection with the

- Animal Model versus Selection within contemporary Groups for Swine, *J. Dairy Sci.*, 73(9):2657-2665
- [26]Muasya, T.K., Ilatsia, E.D., Magothe, T.M., Kahi, A.K., 2007, Heterogeneity of variance and its implications on dairy cattle breeding, *South African Journal of Anim. Sci.*, 37(3):170-175
- [27]Muir William M., Samuel, E., *Poultry Genetics, Breeding and Technology*, p.153
- [28]Nagy Istvan, *Quantitative Genetics*, Chapter 11. BLUP. Kaposvar University, [www.tankonyvtar.hu](http://www.tankonyvtar.hu)
- [29]Nielsen, H.M., Sonesson, A.K., Meuwissen, T.H.E., 2011, Optimum contribution selection using traditional BLUP and genomic breeding values in aquaculture breeding schemes, *J. Anim. Sci.*, 89(3):630-638
- [30]Nishio Motohide, Satoh Masahiro, 2014, Including Dominance Effects in the Genomic BLUP Method for Genomic Evaluation, published January 08, 2014 in *Plos/One*, [www.plosone.org](http://www.plosone.org)
- [31]Ollivier Louis, 1999, On the use of animal models in the analysis of selection experiments, *Genet. Sel. Evol.* 31:135-148
- [32]Pang, H., Wu, C.X., Zhang, Y., Gong, G.F., Bi YH, 1989, Animal model and multiple trait BLUP applied in poultry genetic evaluation, *Yi Chuan Xue Bao*, 16(4):291-298
- [33]Pantelik, V., Plavsic, M., Trivunovic, S., Aleksic, S., Sretenovic, L.J., Ostojic-Andric, D., Niksic, D., 2011, The evaluation of breeding value of Simmental bulls for milk performance in Serbia. *Biotechnology in Animal Husbandry* 27(2):127-135
- [34]Patry Clotilde, Ducrocq Vincent, 2011, Accounting for genomic pre-selection in national BLUP evaluations in dairy cattle, *Genet. Sel., Evol.*, 43(1):30
- [35]Phocas Florence, Laloe Denis, 2004, Should genetic groups be fitted in BLUP evaluation? Practical answer for the French AI beef sires evaluation, *Genet. Sel. Evol.*, 36:325-345
- [36]Piepho, H.P., Mohring, J., Melchinger, A.E., Buchse, A., 2008, BLUP for phenotypic selection in plant breeding and variety testing, *Euphytica* 161:209-228
- [37] Popescu Agatha, 1988, Research regarding the application of BLUP method in bulls' breeding value estimation for meat production. Symposium on „Actualities in Animal Husbandry”, Vol. XIII, Cluj-Napoca, 153-156
- [38]Popescu Janina, Petroman Cornelia, Balan Ioana,, Marin Diana, Heber Loredana, 2009, The individual animal model for many characters in swine, *Scientific Papers, Agricultural Management, Series I, Vol. XI(2)*
- [39]Pullar Duncan, 2001, Genetic Improvement of Beef Cattle-The Scientist, [www.bsas.org.uk](http://www.bsas.org.uk)
- [40]Robinson, G.K., 1991, That BLUP is a Good Thing: The Estimation of Random Effects, *Statistical Science*, 6(10):15-51
- [41] Rosati, A., Tewold, A., Mosconi, C., 2008, *Animal Production and Animal Science Worldwide: WAAP Book of the year 2007*
- [42]Sasaki, Y., 1992, The effectiveness of the best linear unbiased prediction of beef sires using field data collected from small farms. *J. Anim. Sci.*, 70:3317-3321
- [43]Sasaki, Y., Miyake, T., Gaillard, C., Oguni, T., Matsumoto, M., Ito, M., Kurahara, T., Sasae, Y., Fujinake, K., Ohtagaki, S., Dougao, T., 2006, Comparison of genetic gains per year for carcass traits among breeding programs in the Japanese Brown and the Japanese Black Cattle, *J. Anim. Sci.*, 84:317-323
- [44]Schneeberger, M., Barwick, S.A., Crow, G.H., Hammond, K., 2011, Economic indices using breeding values predicted by BLUP, *J. of Anim. Breeding and Genetics*, 109(1-6)
- [45]Searle, S.R., 1982, *Matrix algebra useful for statistics*, Wiley, New York, NY
- [46]Somthep, T., 2002, Genetic improvement in beef and dairy cattle in Thailand: BLUP applications, *Proceedings of the 7th World Congress on Genetics Applied to Livestock Production*, Montpellier, France, August, 2002, Session 25/2002, pp.1-4
- [47]Sonesson Anna K., Gjerde Bjarne, Meuwissen Theo H.E., 2005, Truncation selection for BLUP-EBV and phenotypic values in fish breeding schemes, *Aquaculture*, vol.243(1-4):61-68
- [48]Tavernier Anne, 1988, Advantages of BLUP animal model for breeding value estimation in horses. *Livestock Production Science*, Vol.20(2):149-160
- [49]Thompson Robin, 2008, Estimation of quantitative genetic parameters. *Proceedings of the Royal Society Biological Sciences*
- [50]Tumwasorn, S., Katkasame, S., Kuha, K., 2000, BLUP Base for Dairy Cattle Genetic AI improvement in Thailand, *Asian-Aus. J. Anim. Sci.*, 13 Supplement, July 2000B:155-157
- [51]Van der Werf Julius, *Mixed models for Genetic Analysis*, University of New England, Armidale, NSW, Australia, [www.vsni.co.uk/products/asreml/user/geneticanalysis.pdf](http://www.vsni.co.uk/products/asreml/user/geneticanalysis.pdf)
- [52]Verrier, E., Colleau, J.J., Foulley, J.L., 1993, Long-term effects of selection based on animal model BLUP in a finite population. *Theor. Appl. Genet.* 87:446-454
- [53]Vicovan, P.G., Vicovan, A., Radu, R., Enciu, A., Ida, A., Prediction of breeding value of rams for growth of liveweight by progeny test, evaluated by three methods, *Scientific Papers, Series Animal Science*, Vol.53, Iasi
- [54]Wezyk, S., Jankowski, J., *Mixed Model Methodology: Meat type Birds*, p.150-154
- [55]Wilson Alastair J., Reale, D., Clements Michelle N., Morrissey Michael M., Postma Erik, Walling Craig A., Kruuk Loeske E.B., Nussey Daniel H., 2010, An ecologist guide to the animal model. *J. of Animal Ecology*, 79:13-26
- [56]Xu-Qing Liu, Jian-Ying Rong, Xiu-Ying Liu, 2008, Best linear unbiased prediction for linear combinations in general mixed linear models. *J. of Multivariate Analysis*, 99(8):1503-1517
- [57]Zurovacova, B., Brno, M.Z.L.U., 2008, Performance of Slovak show jumping horses evaluated using BLUP Animal Model, *J. of Agrobiology*, 25:1-4